

# Climate, economics, and statistical thermodynamics

Alastair D. Jenkins

*Uni Research Computing*

*2nd floor, Datablokken*

*Høyteknologisenteret, Thormøhlensgt. 55*

*PO Box 7810, 5020 Bergen, Norway*

*<alastair.jenkins@uni.no>*

*Mini-workshop, climate science and economics*

*Nansen Center, Bergen, 2014-10-13*

# Introduction

- ▶ Earth system modelling: coupling of the physical climate with biogeochemical processes
- ▶ Inclusion of socioeconomic processes: adds another layer of complexity and unpredictability
  - ▶ Particularly since economic actors are 'self-aware': can read scientific papers and model code . . .
- ▶ Nevertheless, both the climate system and economies are subject to physical laws
  - ▶ Large and complex systems, statistical mechanics and thermodynamics should be applicable
  - ▶ Some form of maximum entropy principle?
- ▶ 'Dissipative' system: maximum entropy *production* [Dewar 2003; Martyushev & Seleznev 2006].

# The Big Questions?

- ▶ Is coupled modelling of climate and socioeconomic systems possible?
- ▶ What can we learn from history?
- ▶ How can we analyse and/or specify physical constraints on the system?

# 'Maximum entropy production'

- ▶ Maximum entropy  $S$  for an isolated system in equilibrium:

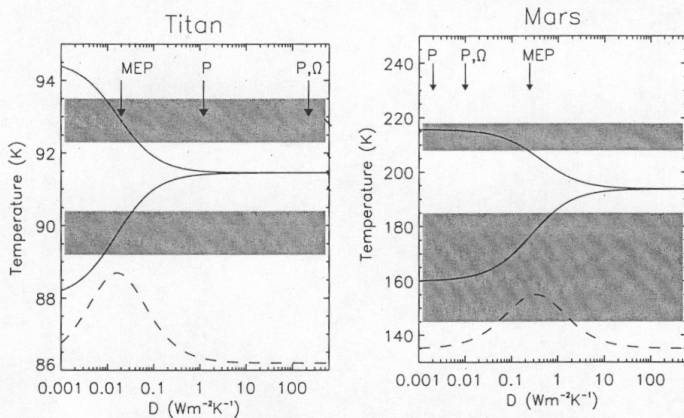
$$dS \geq dQ/T \quad S = k \log W$$

$S$  is entropy,  $Q$  is heat supplied to system,  $k$  is Boltzmann constant,  $W$  is volume in phase space.

- ▶ For a dissipative system subject to appropriate constraints, the most 'probable' state should be that of maximum entropy *production* (MaxEP) [e.g., Dewar 2003].
- ▶ Maximum volume in the phase space of 'paths'.

# MaxEP—applications

- ▶ Transition to turbulence
- ▶ Climate of Earth and other planets [e.g., Lorenz et al. 2001]
- ▶ Effect of large-scale wind power production on the atmospheric circulation [Miller et al. 2011]
- ▶ Feedback between climate and ecology (optimal radiation balance) [Kleidon et al. 2000]



**Figure 2.** Observed temperature contrasts on Titan (a) and Mars (b) agree with predictions at maximum entropy production. Shading indicates observed annually-averaged temperature ranges for the regions 10- 20 deg and 40-60 deg latitude. Solid curves are model temperatures (upper curve tropics; lower curve polar regions) as a function of  $D$ : dashed curves at bottom are the entropy production  $dS/dt=(F/T_1-F/T_0)$  in arbitrary units. It is seen that the temperatures are successfully predicted where  $dS/dt$  has a maximum. Values of  $D$  predicted from scaling pressure ( $P$ ), or pressure and rotation rate ( $P,\Omega$ ) are marked: the arrows marked MEP correspond to the maximum entropy value inferred from the simple expression  $D=\sigma T^3/2$ . High ( $>10\text{Wm}^{-2}\text{K}^{-1}$ ) values for  $D$  predict near-isothermal conditions and do not agree with observations. Low ( $<0.01\text{Wm}^{-2}\text{K}^{-1}$ )  $D$  values appear compatible for Mars but not for Titan, but see text for discussion of the failure of small  $D$  for the Mars case. Note that the temperature slopes are steepest at MEP.

# 'Thermodynamics' / MaxEP in economic modelling

- ▶ Human society consumes energy, raw materials, and the products of biological processes, so can be regarded as a dissipative system.
- ▶ Some economic models consider the 'information entropy' of economic networks
- ▶ But I consider the 'real' thermodynamic entropy, generated by the dissipation of mechanical, chemical energy etc.
- ▶ Examples: Georgescu-Roegen [1971], Lorenz [2003], Jenkins [2004, 2005, 2009], Annala & Salthe [2009], Hermann-Pillath [2010], Woollacott [2011].
- ▶ 'Rebound effect', see Woollacott [2011] and references therein.
  - ▶ MaxEP may explain *increasing* energy consumption after processes become more energy-efficient.

# 'History'

- ▶ It is instructive to consider the entropy production in historical economic systems (agricultural, hydraulic, industrial).
- ▶ It may be valuable to consider the transitions which occurred between different systems (changes in technology, exhaustion of resources, conflict periods, climate change, epidemics, etc.)
- ▶ This speaker [Jenkins 2004, 2009] performed some preliminary calculations for the early whaling activities on Spitsbergen (exhaustion of a non-renewable biological resource).





# 17th-century Svalbard whaling

[Conway 1906]

- ▶ In a good year (1697), 201 ships caught 1968 whales and obtained 63883 casks of blubber (perhaps 13000 tonnes)
- ▶ Lipid content corresponds to  $570 \times 10^{12}$  J, spread over the year this is 18 MW, entropy prod.  $63 \text{ kW K}^{-1}$
- ▶ Compare with the size of a 'typical' country's economy: England 1688 (Gregory King, in Laslett 1971), population 5.5 M, food consumption  $\approx 530\text{--}1000$  MW, entropy prod.  $\approx 1.9\text{--}3.2 \text{ MW K}^{-1}$ .
- ▶ Whale oil was largely used in the making of soap, used to launder fine linen for the elite, thus acting as a 'social catalyst' for the political economy
- ▶ Elite population of England was about 100k, food consumption  $\approx 10\text{--}15$  MW this is of the same order of magnitude as the energy content in the supply of whale lipid to NW Europe

# 17th-century Svalbard whaling

Effect on the marine ecosystem:

- ▶ From Sakshaug 1997, new primary production in Barents Sea is  $60 \text{ g C m}^{-2} \text{ a}^{-1}$
- ▶ Krill and Calanus production is  $9.5 \text{ g C m}^{-2} \text{ a}^{-1}$
- ▶ If 5 g of this is available for whales, and they use it with 10% efficiency to produce lipid for 'harvesting', we get  $0.58 \text{ g lipid m}^{-2} \text{ a}^{-1}$
- ▶ A production of 13000 tonnes thus requires a primary production area of  $22000 \text{ km}^2$

Was this sustainable?

# What do economists *need* from climate scientists? and v.v.?

- ▶ Physical, chemical, biological conditions
  - ▶ Temperature, precipitation, wind, sea level, . . .
  - ▶ Conditions for agriculture, fisheries, transport, building, health
  - ▶ Access to water, minerals and raw materials
  - ▶ Disposal of waste

# What do climate scientists *need* from economists?

- ▶ Social conditions, leading to
  - ▶ Changes in radiation and water balance
  - ▶ Changes in biological environment
  - ▶ Amount of raw material extraction
  - ▶ Amount of environmental pollution

# Discussion points

- ▶ Economic models should be physically consistent
  - ▶ Energy and raw material pathways
  - ▶ Pollution dispersion
  - ▶ Feedback on radiation balance
- ▶ Allow for (potentially sudden) changes in energy and material flows
  - ▶ Alternative pathways with greater entropy production?
- ▶ Scope for analysis of past (historical, archaeological) processes and events?

# References I



A. Annala and S. Salthe.  
Economies evolve by energy dispersal.  
*Entropy*, 11:606–633, 2009.  
doi: 10.3390/e11040606.



M. Conway.  
*No Man's Land. A History of Spitsbergen from its Discovery in 1596 to the Beginning of the Scientific Exploration of the Country.*  
Cambridge University Press, 1906.  
Facsimile edition, Norbok a.s., 1995.



R. L. Dewar.  
Information theory explanation of the fluctuation theorem, maximum entropy production and self-organized criticality in non-equilibrium stationary states.  
*Journal of Physics A: Mathematical and General*, 36:631–641, 2003.  
E-print arXiv:cond-mat/0005382.



N. Georgescu-Roegen.  
*The Entropy Law and the Economic Process.*  
Harvard University Press, Cambridge, MA, U.S.A., 1971.



C. Herrmann-Pillath.  
Rethinking evolution, entropy and economics: A triadic conceptual framework for the Maximum Entropy Principle as applied to the growth of knowledge, 2010.  
ISSN 14369753.  
Frankfurt School of Finance & Management, Working Paper No. 146.

## References II



A. D. Jenkins.

Entropy production, polar ecology and economics.

Presented at Arctic Science Summit Week (ASSW) 2009, Bergen, Norway, 23–28 March 2009.



A. D. Jenkins.

Maximum entropy production and climate change effects.

Poster presented at Bjerknes Centenary Conference 'Climate Change in High Latitudes', Bergen, September 1-3, 2004.



A. D. Jenkins.

Thermodynamics and economics.

Available for download from <http://www.arXiv.org/abs/cond-mat/0503308>, 2005.



A. Kleidon, K. Fraedrich, and M. Heimann.

A green planet versus a desert world: Estimating the maximum effect of vegetation on land surface climate.

*Climate Change*, 44:471–493, 2000.



P. Laslett.

*The World We Have Lost*.

Methuen, London, 1979.



R. Lorenz.

Economics and maximum entropy production, 2003.

*Geophysical Research Abstracts*, vol. 5, paper 12837.



## References III



R. D. Lorenz, J. I. Lunine, C. P. McKay, and P. G. Withers.  
Entropy production by latitudinal heat flow on Titan, Mars and Earth.  
*Geophysical Research Letters*, 28:415–418, 2001.



L. M. Martyushev and V. D. Seleznev.  
Maximum entropy production principle in physics, chemistry and biology.  
426:1–45, 2006.  
doi: 10.1016/j.physrep.2005.12.001.



L. M. Miller, F. Gans, and A. Kleidon.  
Estimating maximum global land surface wind power extractability and associated climatic consequences.  
*Earth System Dynamics*, 2:1–12, 2011.  
doi: 10.5194/esd-2-1-2011.



H. Ozawa, A. Ohmura, R. D. Lorenz, and T. Pujol.  
The second law of thermodynamics and the global climate system: A review of the maximum entropy production principle.  
*Reviews of Geophysics*, 41:4–1–24, 2003.  
doi: 10.1029/2002RG000113.



E. Sakshaug.  
Biomass and productivity distributions and their variability in the Barents Sea.  
*ICES J. Marine Sci.*, 54:341–350, 1997.

## References IV



**J. Woollacott.**

The evolution of energy flows through the economy: A thermodynamic perspective.

Master's thesis, Durham, NC, U.S.A., 2011.